

H.S.C Annual Examinations 2021 MATHEMATICS PAPER I (MODEL PAPER) (Science Pre-engineering & Science General Group)

SECTION "A" (Short- Answers Question)

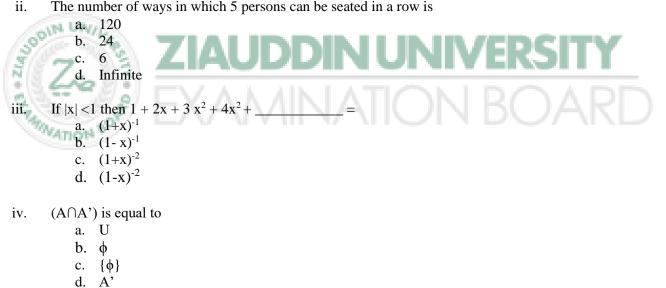
Time: 30 minutes

Max.marks:50

NOTE: This section consists of 25 part questions and all are to be answered.

Q1. Select the correct answer from the given options.

- i. The in radius r of triangle ABC is equal to
 - a. sΔ Δ b. S S c. Δ Δ d. s–a
- ii. The number of ways in which 5 persons can be seated in a row is



- If I is an imaginary number then i³³ v.
 - a. Ι
 - b. —i
 - c. 1
 - d. -i

If z = -3i + 2, then $z + \hat{z} =$ vi.

- a. 6i
- b. 6
- c. 0
- d. 4

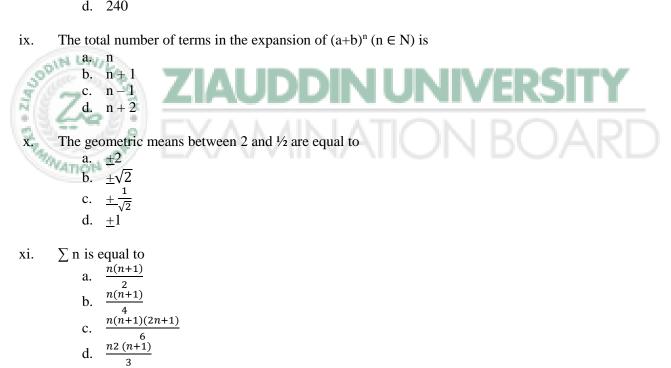
The sum of the roots of the equation $y^2 - 2y + 8 = 0$ vii.

- a. 2
- b. 4
- c. 8
- d. -8

 $\binom{6}{2,3}$ is equal to viii.

- 1 a.
- b. 60
- c. 120
- d. 240

The total number of terms in the expansion of $(a+b)^n (n \in N)$ is



- If 1, x 1, 3 are in A.P then x =xii.
 - a. 2

d.

- b. 1
- c. -2,4
- d. 3

The number of permutations of the letters of the word COMMITTEE is a. $\binom{9}{222}$ b. $\binom{6}{222}$ c. $\binom{9}{221}$ xiii.

If arc length S is equal to the radius r, then the central angle θ is

d. $\binom{222}{9}$

xiv.

- a. 0 radian
- b. $\frac{1}{2}$ radian
- c. 2 radian
- d. 1 radian

In a triangle ABC if $\gamma = 90^{\circ}$ then the law of cosine reduces to xv.

a. $a^2 = b^2 + c^2$ b. $b^2 = a^2 - c^2$ 3 c. $c^2 = a^2 + b^2$ d. $c^2 = a^2 - b^2$ R . di. xvi lt rcos If $r\cos\theta = 4$ and $r\sin\theta = 3$ then r =b. 5 c. 6 d. 2

xvii. A coin tossed thrice. The probability of getting three tail is

> $\frac{1}{23}$ $\frac{21}{82}$ $\frac{82}{3}$ a. b. c. d.

 $1-2\sin^2\frac{\theta}{2}$ is equal to xviii.

a. $\sin \theta$ b. $\cos \theta$ $\frac{\sin \frac{\theta}{2}}{\cos \frac{\theta}{2}}$ c. d.

The angle 135° in radians is xix.

5π a. 4 3π b. $\frac{4}{2\pi}$ c. 4 d. 135π xx. The period of sin x is

- a. π/2
- b. π
- с. т
- d. 2π

xxi. If roots of the equation $ax^2 + bx + c = 0$ are real then $b^2 - 4ac$ is

- a. Positive b. Negative c. Zero d. Perfect square Tan $(180^{\circ} - \theta) =$ a. tan θ b. $- \tan \theta$ c. cot θ d. perfect square
 - d. $-\cot \theta$
- xxiii. If ω is a complex cube of unity then $(1 + \omega + \omega^2)^2$ will be equal to
 - a. 0
 - b. 1
 - c. 4
 - d. ω^2

xxiv. $1/1+tan^2 \theta$

- a. $\sec^2 \theta$
- b. $\cos^2 \theta$
- c. $\sin^2 \theta$
- d. $\cot^2 \theta$

xxv. Area of a triangle ABC is

- a. $\frac{1}{2}$ ab sin β
- b. $\frac{1}{2}$ bc sin α
- c. $\frac{1}{2} \operatorname{ac} \sin \gamma$
- d. $\frac{1}{2}$ bc sin β

(30 marks)

Time: 1hour 30 minutes

NOTE: Attempt any THREE questions from this section. All questions carry equal marks.

2.

- (a) If $z_1 = 1 + i$ and $z_2 = 3 2i$, find the value of $|5z_1 4z_2|$ and $\frac{z_1}{z_2}$
- (b) Show that the multiplication is a binary operation on $S = \{1, -1, i, -i\}$ is multiplication commutative and associative in S?

3.

(a) If α and β are the roots of given px²+qx+r=0, form an equation whose roots are $\frac{\alpha}{\beta}$ and $\frac{\beta}{\alpha}$.

- (b) If a point on the rim of a 21cm, diameter fly wheel travels 5040 meters in a minute, through how many radians does the wheel turn in a second?
- (a) Solve $\sin \theta + \cos \theta = 1$
- (b) Prove by mathematical induction that $2 + 6 + 12 + \ldots + n (n+1) = \frac{1}{3}n (n+1) (n+2)$

5.

4.

(a) Write in the simplified form the term independent of x in $(x-2/x)^{10}$

(b) How many different arrangements can be made by using all the letters of the word

"MATHEMATICS" how many of them begin with "C"? How many of them begin with T? in

how many of them consonants will occur together?

6.

- (a) Prove that. (any TWO)
- (i) $\cos 3\theta = 4\cos^3 \theta 3\cos \theta$

(ii)
$$\sin(\theta + \phi) \sin(\theta - \phi) = \sin^2 \theta - \sin^2 \phi$$

(iii)
$$\frac{\sin 3\theta}{\sin \theta} - \frac{\cos 3\theta}{\cos \theta} = 2$$

(b) Prove that $=\frac{1}{r^2} + \frac{1}{r1^2} + \frac{1}{r2^2} + \frac{1}{r3^2} = \frac{a^2 + b^2 + c^2}{\Delta^2}$

Section "C" (Detailed – Answer Questions). (20 marks)

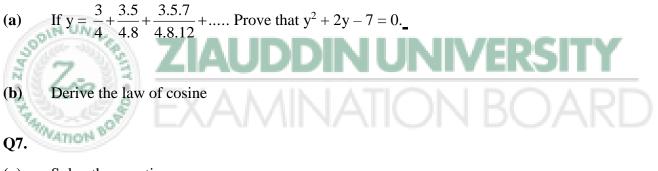
NOTE: Attempt two questions from this section including question number 7 which is compulsory.

7.

- (a) The sum of four terms in an A. P is 4. The sum of the products of the first and last terms and of two middle terms is -38. Find the numbers.
- (b) Find the value of "n" so that $\underline{a^{n+1} + b^{n+1}}$ may become the G.M b/w a and b.

 $a^n + b^n$

Q.6



(a) Solve the equation

4x + 3t = 25

$$\frac{4}{x} + \frac{3}{t} = 2$$

(**b**) If α , β are the roots of pt²+qt+q=0 prove that

$$\sqrt{q/p} + \sqrt{\alpha/\beta} + \sqrt{\beta/\alpha} = 0$$